

# Hybrid Multiobjective evolutionary Algorithm Based Technique for Economic Emission Load Dispatch Optimization Problem

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## Abstract:

In This paper, we present a hybrid approach combining two optimization techniques for solving Economic Emission Load Dispatch Optimization Problem EELD. The EELD problem is formulated as a nonlinear constrained multiobjective optimization problem with both equality and inequality constraints. Our approach integrates the merits of both genetic algorithm (GA) and local search (LS). The proposed approach employs the concept of co-evolution and repair algorithm for handling nonlinear constraints. Also, it maintains a finite-sized archive of non-dominated solutions which gets iteratively updated in the presence of new solutions based on the concept of  $\varepsilon$ -dominance. The use of  $\varepsilon$ -dominance also makes the algorithms practical by allowing a decision maker to control the resolution of the Pareto set approximation. To improve the solution quality we implement local search (LS) technique as neighborhood search engine where it intends to explore the less-crowded area in the current archive to possibly obtain more nondominated solutions.

Several optimization runs of the proposed approach are carried out on the standard IEEE 30-bus 6-generator test system. Simulation results with the proposed approach have been compared to those reported in the literature. The comparison demonstrates the superiority of the proposed approach and confirms its potential to solve the multiobjective EELD problem.

**Keywords:** Economic emission load dispatch; Evolutionary algorithms; Multiobjective optimization, Local search.

## 1. Introduction.

The purpose of EELD problem is to figure out the optimal amount of the generated power for the fossil-based generating units in the system by minimizing the fuel cost and emission level simultaneously, subject to various equality and inequality constraints including the security measures of the power transmission/distribution. Various optimization techniques have been proposed by many researchers to deal with this multiobjective programming problem with varying degree of success.

Different techniques have been reported in the literature pertaining to economic emission load dispatch problem. In [5,12] the problem has been reduced to a single objective problem by treating the emission as a constraint with a permissible limit. This formulation, however, has a severe difficulty in getting the trade-off relations between cost and emission. Alternatively, minimizing the emission has been handled as another objective in addition to usual cost

objective. A linear programming based optimization procedures in which the objectives are considered one at a time was presented in [10]. Unfortunately, the EELD problem is a highly nonlinear and a multimodal optimization problem. Therefore, conventional optimization methods that make use of derivatives and gradients, in general, not able to locate or identify the global optimum. On the other hand, many mathematical assumptions such as analytic and differential objective functions have to be given to simplify the problem. Furthermore, this approach does not give any information regarding the trade-offs involved.

In other research direction, the multiobjective EELD problem was converted to a single objective problem by linear combination of different objectives as a weighted sum [6,9,25,26]. The important aspect of this weighted sum method is that a set of Pareto-optimal solutions can be obtained by varying the weights. Unfortunately, this requires multiple runs as many times as the number of desired Pareto-optimal solutions. Furthermore, this method cannot be used to find Pareto-optimal solutions in problems having a nonconvex Pareto-optimal front. In addition, there is no rational basis of determining adequate weights and the objective function so formed may lose significance due to combining noncommensurable objectives. To avoid this difficulty, the  $\varepsilon$ -constraint method for multiobjective optimization was presented in [15,24]. This method is based on optimization of the most preferred objective and considering the other objectives as constraints bounded by some allowable levels. These levels are then altered to generate the entire Pareto-optimal set. The most obvious weaknesses of this approach are that it is time-consuming and tends to find weakly nondominated solutions.

Goal programming method was also proposed for multiobjective EELD problem [17]. In this method, a target or a goal to be achieved for each objective is assigned and the objective function will then try to minimize the distance from the targets to the objectives. Although the method is computationally efficient, it will yield an inferior solution rather than a noninferior one if the goal point is chosen in the feasible domain. Hence, the main drawback of this method is that it requires a priori knowledge about the shape of the problem search space.

Heuristic algorithms such as genetic algorithm have been recently proposed for solving OPF problem [4,22,23]. The results reported were promising and encouraging for further research. Moreover the studies on heuristic algorithms over the past few years, have shown that these methods can be efficiently used to eliminate most of difficulties of classical methods [1-3,8,11]. Since they are population-based techniques, multiple Pareto-optimal solutions can, in principle, be found in one single run.

In this paper a new hybrid multiobjective approach is proposed, which based on concept of co-evolution and repair algorithm for handling constraints. It is based on the  $\varepsilon$ -dominance concept which maintains a finite-sized archive of non-dominated solutions which gets iteratively updated according to the chosen  $\varepsilon$ -vector. Also, LS method is introduced as neighborhood search engine where it intends to explore the less-crowded area in the current archive to possibly obtain more nondominated solutions.

## 2. Multiobjective Optimization

Multiobjective optimization differs from the single objective case in several ways:

- The usual meaning of the optimum makes no sense in the multiple objective case because the solution optimizing all objectives simultaneously is, in general, impractical; instead, a search is launched for a feasible solution yielding the best compromise among objectives on a set of, so called, efficient solutions;
- The identification of a best compromise solution requires taking into account the preferences expressed by the decision-maker;

- The multiple objectives encountered in real-life problems are often mathematical functions of contrasting forms.
- A key element of a goal programming model is the achievement function; that is, the function that measures the degree of minimization of the unwanted deviation variables of the goals considered in the model. A general multiobjective optimization problem is expressed by:

MOP :

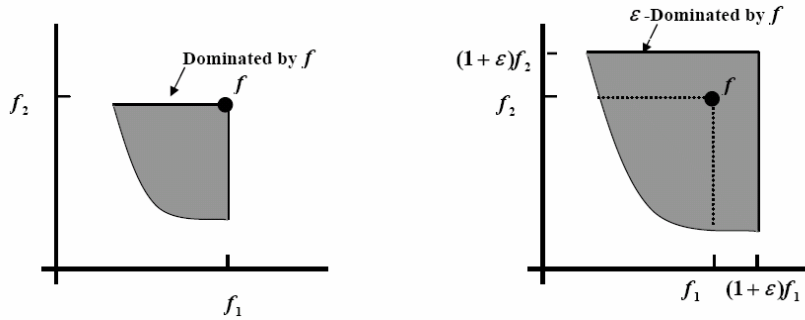
$$\begin{aligned} \text{Min } F(x) &= (f_1(x), f_2(x), \dots, f_m(x))^T \\ \text{s.t. } & x \in S \\ & x = (x_1, x_2, \dots, x_n)^T \end{aligned}$$

Where  $(f_1(x), f_2(x), \dots, f_m(x))$  are the  $m$  objectives functions,  $(x_1, x_2, \dots, x_n)$  are the  $n$  optimization parameters, and  $S \in R^n$  is the solution or parameter space.

**Definition 1.** (Pareto optimal solution):  $x^*$  is said to be a Pareto optimal solution of MOP if there exists no other feasible  $x$  (i.e.,  $x \in S$ ) such that,  $f_j(x) \leq f_j(x^*)$  for all  $j = 1, 2, \dots, m$  and  $f_j(x) < f_j(x^*)$  for at least one objective function  $f_j$ .

**Definition 2 [18].** ( $\epsilon$ -dominance) Let  $f : x \rightarrow R^m$  and  $a, b \in X$ . Then  $a$  is said to  $\epsilon$ -dominate  $b$  for some  $\epsilon > 0$ , denoted as  $a \succ_\epsilon b$ , if and only if for  $i \in \{1, \dots, m\}$

$$(1 + \epsilon)f_i(a) \geq f_i(b)$$



**Fig. 1:** Graphs visualizing the concepts of dominance (left) and  $\epsilon$ -dominance (right).

**Definition 3 [18].** ( $\epsilon$ -approximate Pareto set) Let  $X$  be a set of decision alternatives and  $\epsilon > 0$ . Then a set  $x_\epsilon$  is called an  $\epsilon$ -approximate Pareto set of  $X$ , if any vector  $a \in x$  is  $\epsilon$ -dominated by at least one vector  $b \in x_\epsilon$ , i.e.,

$$\forall a \in x : \exists b \in x_\epsilon \text{ such that } b \succ_\epsilon a$$

According to definition 2, the  $\epsilon$  value stands for a relative “tolerance” allowed for the objective values which declared in figure 1. This is especially important in higher dimensional objective spaces, where the concept of  $\epsilon$ -dominance can reduce the required number of solutions considerably. Also, the use of  $\epsilon$ -dominance also makes the algorithms practical by allowing a decision maker to control the resolution of the Pareto set approximation by choosing an appropriate  $\epsilon$  value.

### 3. Economic Emission Load Dispatch (EELD)

The economic emission load dispatch involves the simultaneous optimization of fuel cost and emission objectives which are conflicting ones. The deterministic problem is formulated as described below.

### 3.1 Objective Functions

**Fuel Cost Objective.** The classical economic dispatch problem of finding the optimal combination of power generation, which minimizes the total fuel cost while satisfying the total required demand can be mathematically stated as follows [24]:

$$f(\cdot) = C_t = \sum_{i=1}^n C_i(P_{Gi}) = \sum_{i=1}^n (a_i + b_i P_{Gi} + c_i P_{Gi}^2) \$ / hr$$

Where

$C$ : total fuel cost (\$/hr),  $C_i$ : is fuel cost of generator  $i$   $P_{Gi}$ : power generated (p.u) by generator  $i$ ,  
 $a_i, b_i, c_i$ : fuel cost coefficients of generator  $i$ ,  $n$ : number of generator.

**Emission Objective.** The emission function can be presented as the sum of all types of emission considered, such as  $NO_x, SO_2$ , thermal emission, etc., with suitable pricing or weighting on each pollutant emitted. In the present study, only one type of emission  $NO_x$  is taken into account without loss of generality. The amount of  $NO_x$  emission is given as a function of generator output, that is, the sum of a quadratic and exponential function:

$$f_2(\cdot) = E_{NO_x} = \sum_{i=1}^n [10^{-2}(\alpha_i + \beta_i P_{Gi} + \gamma_i P_{Gi}^2) + \xi_i \exp(\lambda_i P_{Gi})] ton / hr$$

Where,  $\alpha_i, \beta_i, \gamma_i, \xi_i, \lambda_i$ : coefficients of the  $i$ th generator's  $NO_x$  emission characteristic.

### 3.2 Constraints

The optimization problem is bounded by the following constraints:

- **Power balance constraint.** The total power generated must supply the total load demand and the transmission losses.

$$\sum_{i=1}^n P_{Gi} - P_D - P_{Loss} = 0$$

Where  $P_D$ : total load demand (p.u.), and  $P_{loss}$ : transmission losses (p.u.).

The transmission losses are given by[13]:

$$P_{Loss} = \sum_{i=1}^n \sum_{j=1}^n [A_{ij} (P_i P_j + Q_i Q_j) + B_{ij} (Q_i P_j - P_i Q_j)]$$

Where  $P_i = P_{Gi} - P_{Di}$ ,  $Q_i = Q_{Gi} - Q_{Di}$ ,  $A_{ij} = \frac{R_{ij}}{V_i V_j} \cos(\delta_i - \delta_j)$ ,  $B_{ij} = \frac{R_{ij}}{V_i V_j} \sin(\delta_i - \delta_j)$

$n$ : number of buses

$\delta_i$ : voltage angle at bus  $i$

$R_{ij}$ : series resistance connecting buses  $i$  and  $j$

$P_i$ : real power injection at bus  $i$

$V_i$ : voltage magnitude at bus  $i$

$Q_i$ : reactive power injection at bus  $i$

- **Maximum and Minimum Limits Of Power Generation.** The power generated  $P_{Gi}$  by each generator is constrained between its minimum and maximum limits, i.e.,

$$P_{Gi \min} \leq P_{Gi} \leq P_{Gi \max}, \quad Q_{Gi \min} \leq Q_{Gi} \leq Q_{Gi \max}, \quad V_{i \min} \leq V_i \leq V_{i \max}, \quad i = 1, \dots, n$$

where  $P_{Gi \min}$ : minimum power generated, and  $P_{Gi \max}$ : maximum power generated.

- **Security Constraints.** A mathematical formulation of the security constrained EELD problem would require a very large number of constraints to be considered. However, for typical systems the large proportion of lines has a rather small possibility of becoming overloaded. The EELD problem should consider only the small proportion of lines in violation, or near violation of their respective security limits which are identified as the critical lines. We consider only the critical lines that are binding in the optimal solution. The detection of the critical lines is assumed done by the experiences of the DM. An improvement in the security can be obtained by minimizing the following objective function.

$$S = f(P_{Gi}) = \sum_{j=1}^k (|T_j(P_G)| / T_j^{\max})$$

Where,  $T_j(P_G)$  is the real power flow  $T_j^{\max}$  is the maximum limit of the real power flow of the  $j$  th line and  $k$  is the number of monitored lines. The line flow of the  $j$  th line is expressed in terms of the control variables  $P_{Gs}$ , by utilizing the generalized generation distribution factors (GGDF) [20] and is given below.

$$T_j(P_G) = \sum_{i=1}^n (D_{ji} P_{Gi})$$

where,  $D_{ji}$  is the generalized GGDF for line  $j$ , due to generator  $i$

For secure operation, the transmission line loading  $S_\ell$  is restricted by its upper limit as

$$S_\ell \leq S_{\ell \max}, \ell = 1, \dots, n_\ell$$

Where  $n_\ell$  is the number of transmission line.

#### 4. Multiobjective Formulation of EELD Problem.

The multiobjective EELD optimization problem is therefore formulated as:

$$\text{Min } f_1(x) = C_t = \sum_{i=1}^n (a_i + b_i P_{Gi} + c_i P_{Gi}^2) \text{ \$ / hr}$$

$$\text{Min } f_2(\cdot) = E_{NO_x} = \sum_{i=1}^n [10^{-2} (\alpha_i + \beta_i P_{Gi} + \gamma_i P_{Gi}^2) + \xi_i \exp(\lambda_i P_{Gi})] \text{ ton / hr}$$

$$\text{s.t. } \begin{aligned} \sum_{i=1}^n P_{Gi} - P_D - P_{Loss} &= 0, \\ S_\ell &\leq S_{\ell \max}, & \ell &= 1, \dots, n_{Line}, \\ P_{Gi \min} &\leq P_{Gi} \leq P_{Gi \max} & i &= 1, \dots, n, \\ Q_{Gi \min} &\leq Q_{Gi} \leq Q_{Gi \max} & i &= 1, \dots, n, \\ V_{i \min} &\leq V_i \leq V_{i \max} & i &= 1, \dots, n \end{aligned}$$

#### 5. The proposed Algorithm

Recently, the studies on evolutionary algorithms have shown that these algorithms can be efficiently used to eliminate most of the difficulties of classical methods which can be summarized as :

- An algorithm has to be applied many times to find multiple Pareto-optimal solutions.
- Most algorithms demand some knowledge about the problem being solved.
- Some algorithms are sensitive to the shape of the Pareto-optimal front.
- The spread of Pareto-optimal solutions depends on efficiency of the single objective optimizer.

It is worth mentioning that the goal of a multiobjective optimization problem is not only guide the search towards Pareto-optimal front but also maintain population diversity.

### 5.1. Initialization Stage

The algorithm uses two separate population, the first population  $P^{(t)}$  consists of the individuals which initialized randomly satisfying the search space (The lower and upper bounds), while the second population  $R^{(t)}$  consists of reference points which satisfying all constraints. However, in order to ensure convergence to the true Pareto-optimal solutions, we concentrated on how elitism could be introduced in the algorithm. So, we propose an *archiving/selection* [18] strategy that guarantees at the same time progress towards the Pareto-optimal set and a covering of the whole range of the non-dominated solutions. The algorithm maintains an externally finite-sized archive  $A^{(t)}$  of non-dominated solutions which gets iteratively updated in the presence of new solutions based on the concept of  $\varepsilon$ -dominance.

### 5.2. Repair Algorithm

The idea of this technique is to separate any feasible individuals in a population from those that are infeasible by repairing infeasible individuals. This approach co-evolves the population of infeasible individuals until they become feasible. Repair process works as follows. Assume, there is a search point  $\omega \notin S$  (where  $S$  is the feasible space). In such a case the algorithm selects one of the reference points (Better reference point has better chances to be selected), say  $r \in S$  and creates random points  $\bar{Z}$  from the segment defined between  $\omega, r$ , but the segment may be extended equally on both sides determined by a user specified parameter  $\mu \in [0,1]$ . Thus, a new feasible individual is expressed as:

$$z_1 = \gamma.\omega + (1 - \gamma).r, \quad z_2 = (1 - \gamma).\omega + \gamma.r$$

Where  $\gamma = (1 + 2\mu)\delta - \mu$  and  $\delta \in [0,1]$  is a random generated number

### 5.3. LS stage

In this stage, we present modified local search technique (MLS) to improve the solution quality and to explore the less-crowded area in the external archive to possibly obtain more nondominated solutions nearby. We propose a MLS, which is a modification of Hooke and Jeeves method[14] to be suitable for MOP. The general procedure of the MLS techniques can be described by the following steps.

**Step 1.** Start with an arbitrarily chosen point  $(X_m \in \square^n) \in E^t$ , and the prescribed step lengths

$\Delta x_i$  in each of the coordinate directions  $u_i, i = 1, 2, \dots, n$ . Set  $m = 0$ , assume that  $m$  is the size of  $E^t$ .

**Step 2.** Set  $m = m + 1$ , and  $k = 1$  where  $k$  is number of trial (s.t.,  $k = 1, \dots, k_{\max}$ ) to obtain preferred solution than  $X_m$ .

**Step 3.** The variable  $x_i$  is perturbed about the current temporary base point  $X_m$  to obtain the new temporary base point  $X'_m$  as :

$$X'_m = \begin{cases} X_m + \Delta x_i u_i & \text{if } f^+(\cdot) \succ f \\ X_m - \Delta x_i u_i & \text{if } f^-(\cdot) \succ (f(\cdot) \wedge f^+(\cdot)) \\ X_m & \text{if } f(\cdot) \succ (f^+(\cdot) \wedge f^-(\cdot)) \end{cases} \quad \forall i=1,2,\dots,n$$

Where,  $f(\cdot) = f(X_m)$ ,  $f^+(\cdot) = f(X_m + \Delta x_i u_i)$ , and  $f^-(\cdot) = f(X_m - \Delta x_i u_i)$ . Assume  $f(\cdot)$  is the evaluation of the objective functions at a point.

**Step 4.** If the point  $X_m$  unchanged.

- While the number of trial  $k$  not satisfied, reduce the step length  $\Delta x_i$ . The following dynamic equation is presented to reduce  $\Delta x_i$ ,

$$\Delta x_i = \Delta x_i \left( 1 - (r)^{\frac{k}{k_{\max}}} \right), \quad r \in [0,1]$$

and go to step 3.

**Step 5.** Else, if  $X'_m$  is preferred than  $X_m$  (i.e.,  $f(X'_m) \succ f(X_m)$ ),

- The new base point is  $X'_m$ .

**Step 6.** With the help of the base points  $X_m$  and  $X'_m$ , establish a pattern direction  $S$  as

$$S = X'_m - X_m$$

and find a point  $X''_m$  as  $X''_m = X'_m + \lambda S$ , Where  $\lambda$  is the step length, (taken as 1).

**Step 7.** If  $f(X''_m) \succ f(X'_m)$  set  $X_m = X'_m$ ,  $X'_m = X''_m$ , and go to 6.

**Step 8.** If  $f(X''_m) \not\succeq f(X'_m)$  set  $X_m = X'_m$ , and go to 4.

These steps is implemented on all nondominated solutions in  $A^t$  to get the true Pareto optimal solution and to explore the less-crowded area in the external archive. Figure 2 shows the pseudo code of the MLS algorithm.

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**LS technique**

Start with  $X_m \in E^t$

Generate  $X'_m$

While ( $f(X'_m) \not\succeq f(X_m)$ ) | stopped criterion satisfied )

DO

    If  $X'_m = X_m$

        Reduce  $\Delta x_i \rightarrow$  Generate  $X'_m$

    End

    Establish a pattern direction  $S \rightarrow$  Generate  $X''_m$

    If  $f(X''_m) \succ f(X'_m)$ , set  $X_m = X'_m$ ,  $X'_m = X''_m$

        Set  $S \rightarrow$  Generate  $X''_m$

    Else if  $f(X''_m) \not\succeq f(X'_m)$

$X_m = X'_m$

    End

End

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**Fig.2 :** The pseudo code of the MLS algorithm

#### 5.4. Basic Algorithm

It uses two separate population, the first population  $P^{(t=0)}$  (where  $t$  is the iteration counter) consists of the individuals which initialized randomly satisfying the search space, while the

second population  $\mathbf{R}^{(t)}$  consists of reference points which satisfying all constraints. Also, it stores initially the Pareto-optimal solutions externally in a finite sized archive of non-dominated solutions  $\mathbf{A}^{(0)}$ . We use cluster algorithm[7] to create the next population  $\mathbf{P}^{(t+1)}$ , if  $|\mathbf{P}^{(t)}| > |\mathbf{A}^{(t)}|$  (i.e., the size of the population  $\mathbf{P}^{(t)}$  greater than the size of archive  $\mathbf{A}^{(t)}$ ) then new population  $\mathbf{P}^{(t+1)}$  consists of all individual from  $\mathbf{A}^{(t)}$  and the population  $\mathbf{P}^{(t)}$  are considered for the clustering procedure to complete  $\mathbf{P}^{(t+1)}$ , if  $|\mathbf{P}^{(t)}| < |\mathbf{A}^{(t)}|$  then  $|\mathbf{P}|$  solutions are picked up at random from  $\mathbf{A}^{(t)}$  and directly copied to the new population  $\mathbf{P}^{(t+1)}$ .

Since our goal is to find new nondominated solutions, one simple way to combine multiple objective functions into a scalar fitness function is the following weighted sum approach:

$$f(x) = w_1 f_1(x) + \dots + w_i f_i(x) + \dots + w_m f_m(x) = \sum_{j=1}^m w_j f_j(x)$$

Where  $x$  is a string (i.e., individual),  $f(x)$  is a combined fitness function,  $f_i(x)$  is the  $i$ th objective function. When a pair of strings is selected for a crossover operation, we assign a random number to each weight as follows.

$$w_i = \frac{\text{random}_i(.)}{\sum_{j=1}^m \text{random}_j(.)}, \quad i = 1, 2, \dots, m$$

Calculate the fitness value of each string using the random weights  $w_i$ . Select a pair of strings from the current population according to the following selection probability  $\beta(x)$  of a string  $x$  in the population  $\mathbf{P}^{(t)}$

$$\beta(x) = \frac{f(x) - f_{\min}(\mathbf{P}^{(t)})}{\sum_{x \in \mathbf{P}^{(t)}} \{f(x) - f_{\min}(\mathbf{P}^{(t)})\}}, \quad \text{where } f_{\min}(\mathbf{P}^{(t)}) = \min \{f(x) | x \in \mathbf{P}^{(t)}\}$$

This step is repeated for selecting  $|\mathbf{P}|/2$  Paris of strings from the current populations. For each selected pair apply crossover operation to generate two new strings, for each strings generated by crossover operation, apply a mutation operator with a prespecified mutation probability. The system also includes the survival of some of the good individuals without crossover or selection. This method seems to be better than the others if applied constantly.

Algorithm in Table 2, shows the proposed algorithm. The purpose of the function **generate** is to generate a new population in each iteration  $t$ , possibly using the contents of the old population  $\mathbf{P}^{(t-1)}$  and the old archive set  $\mathbf{A}^{(t-1)}$  in associated with variation (recombination and mutation). The function **update** gets the new population  $\mathbf{P}^{(t)}$  and the old archive set  $\mathbf{A}^{(t-1)}$  and determines the updated one, namely  $\mathbf{A}^{(t)}$  as indicated in table 1. The function  $L_s$  is to explore the less-crowded area in the current archive to possibly obtain more nondominated solutions.

The algorithm maintains a finite-sized archive of non-dominated solutions which gets iteratively updated in the presence of a new solutions based on the concept of  $\varepsilon$ -dominance, such that new solutions are only accepted in the archive if they are not  $\varepsilon$ -dominated by any other element in the current archive (table 1), The use of  $\varepsilon$ -dominance also makes the algorithms practical by allowing a decision maker to control the resolution of the Pareto set approximation by choosing an appropriate  $\varepsilon$  value.



**Table 1:** Algorithm of select operator

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1. *INPUT*  $A, x$
2.  $D \leftarrow \{x' \in A: \text{box}(x) \succ \text{box}(x')\}$
3. if  $D \neq \emptyset$  then
4.  $A' \leftarrow A \cup \{x\} \setminus D$
5. else if  $\exists x': (\text{box}(x') = \text{box}(x) \wedge x \succ x')$  then
6.  $A' \leftarrow A \cup \{x\} \setminus \{x'\}$
7. else if  $\exists x': (\text{box}(x') \succeq \text{box}(x))$  then
8.  $A' \leftarrow A \cup \{x\}$
9. else
10.  $A' \leftarrow A$
11. *endif*
12. *OUTPUT*  $A'$

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**Table 2:** Algorithm of the proposed algorithm

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1.  $t \leftarrow 0$
2. Create  $P^{(0)}, R^{(0)}$
3.  $A^{(0)} = \text{nondominated}(P^{(0)})$
3. *while* terminate  $(A^{(t)}, t) = \text{false}$  do
4.  $t \leftarrow t + 1$
5.  $P^{(t)} \leftarrow \text{generate}(A^{(t-1)}, P^{(t-1)})$  {generate new search point}
6.  $A^{(t)} \leftarrow \text{update}(A^{(t-1)}, P^{(t)})$  {update archive (table 1)}
7. *end while*
8.  $A^{(t)} = LS(A^{(t)})$
9. Output :  $A^{(t)}$

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## 6. Implementation of the Proposed Approach

The described methodology is applied to the standard IEEE 30-bus 6-generator test system to investigate the effectiveness of the proposed approach. The values of fuel cost and emission coefficients are given in Table 3. For comparison purposes with the reported results, the system is considered as losses and the security constraint is released. The techniques used in this study were developed and implemented on 1.7-MHz PC using MATLAB environment. Table 4 lists the parameter setting used in the algorithm for all runs.

**Table 3:** Generator cost and emission coefficients

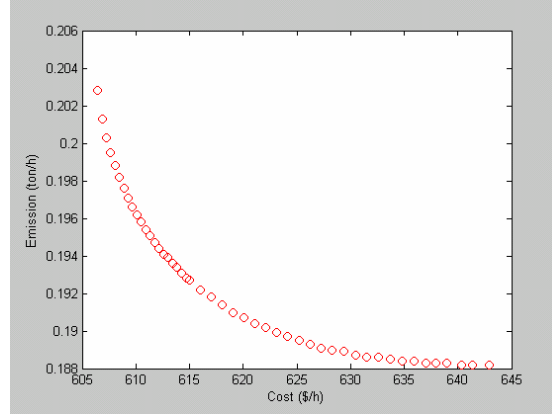
		G1	G2	G3	G4	G5	G6
<b>Cost</b>	a	10	10	20	10	20	10
	b	200	150	180	100	180	150
	c	100	120	40	60	40	100
<b>Emission</b>	$\alpha$	4.091	2.543	4.258	5.426	4.258	6.131
	$\beta$	-5.554	-6.047	-5.094	-3.550	-5.094	-5.555
	$\gamma$	6.490	4.638	4.586	3.380	4.586	5.151
	$\zeta$	2.0E-4	5.0E-4	1.0E-6	2.0E-3	1.0E-6	1.0E-5
	$\lambda$	2.857	3.333	8.000	2.000	8.000	6.667

**Table 4:** GA parameters

Population size (N)	60
No. of Generation	200
Crossover probability	0.98
Mutation probability	0.02
Selection operator	Roulette Wheel
Crossover operator	BLX- $\alpha$
Mutation operator	Polynomial mutation
Relative tolerance $\epsilon$	10e-6

## 7. Results and Discussions

Fig. 3 shows well-distributed Pareto optimal nondominated solutions obtained by the proposed algorithm after 200 generations.



**Fig. 3:** Pareto-optimal front of the proposed approach.

Table 5 and 6 show the best fuel cost and best  $NO_x$  emission obtained by proposed algorithm as compared to Nondominated Sorting Genetic Algorithm (NSGA) [1], Niche Pareto Genetic Algorithm (NPGA) [2] and Strength Pareto Evolutionary Algorithm (SPEA) [3]. It can be deduced that the proposed algorithm finds comparable minimum fuel cost and comparable minimum  $NO_x$  emission to the three evolutionary algorithms.

**Table 5:** Best fuel cost

	NSGA	NPGA	SPEA	Proposed
$P_{G1}$	0.1168	0.1245	0.1086	0.1737
$P_{G2}$	0.3165	0.2792	0.3056	0.3568
$P_{G3}$	0.5441	0.6284	0.5818	0.5411
$P_{G4}$	0.9447	1.0264	0.9846	0.9490
$P_{G5}$	0.5498	0.4693	0.5288	0.4529
$P_{G6}$	0.3964	0.39993	0.3584	0.3715
Best cost	<b>608.245</b>	<b>608.147</b>	<b>607.807</b>	<b>606.4523</b>
Corresponding Emission	0.21664	0.22364	0.22015	0.20280

**Table 6:** Best  $NO_x$  Emission

	NSGA	NPGA	SPEA	Proposed
$P_{G1}$	0.4113	0.3923	0.4043	0.3885
$P_{G2}$	0.4591	0.4700	0.4525	0.4984
$P_{G3}$	0.5117	0.5565	0.5525	0.5167
$P_{G4}$	0.3724	0.3695	0.4079	0.4502
$P_{G5}$	0.5810	0.5599	0.5468	0.5205
$P_{G6}$	0.5304	0.5163	0.5005	0.5005
Best Emission.	<b>0.19432</b>	<b>0.19424</b>	<b>0.19422</b>	<b>0.1882</b>
Corresponding Cost	647.251	645.984	642.603	642.8976

## 8. Conclusion

The approach presented in this paper was applied to economic emission load dispatch optimization problem formulated as multiobjective optimization problem with competing fuel cost, and emission. The algorithm maintains a finite-sized archive of non-dominated solutions which gets iteratively updated in the presence of new solutions based on the concept of  $\epsilon$ -dominance. Moreover, local search is employed to explore the less-crowded area in the current

archive to possibly obtain more nondominated solutions. The following are the significant contributions of this paper:

- (a) The proposed technique has been effectively applied to solve the EELD considering two objectives simultaneously, with no limitation in handling more than two objectives.
- (b) The non-dominated solutions in the obtained Pareto-optimal set are well distributed and have satisfactory diversity characteristics.
- (c) Allowing a decision maker to control the resolution of the Pareto set approximation by choosing an appropriate  $\varepsilon$  value
- (d) The proposed approach is efficient for solving nonconvex multiobjective optimization problems where multiple Pareto-optimal solutions can be found in one simulation run.
- (e) Local search method is employed to explore the less-crowded area in the current archive to possibly obtain more nondominated solutions.
- (f) This work may be very valuable for on-line operation of power systems when environmental constraints are also need to be considered. In addition to on-line operation, this work can be a part of an off-line planning tool when there are hard limits on how much emission is acceptable by a utility over a period of a month or a year.

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